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Symmetry Transformations of IIB Superstring in $\text{AdS}_5 \times S^5$

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Abstract

The $\text{PSU}(2, 2|4)$ transformation laws of the IIB superstring theory in the $\text{AdS}_5 \times S^5$ background are explicitly obtained for the light-cone gauge in the Green-Schwarz formalism.

超弦理論から導き出される時空は10次元である。これを4次元時空の理論と関係づけるためには、時空のコンパクト化が必要である。時空を曲率が負の時空と正の空間に分解するコンパクト化が可能であり、それは5次元反ド・ジッター時空と5次元球面の直積からなる10次元空間である。この場合、現実の時空は反ド・ジッター時空の境界に存在する。反ド・ジッター時空には重力場が存在するため、超弦理論を重力の背景場が存在するときに拡張しなければならない。現在知られている理論は、光円錐ゲージをとったGreen-Schwarz形式の作用を用いる理論である。この論文では、上記の作用から作られるIIB型超弦理論の $\text{PSU}(2, 2|4)$ 対称性変換の形を具体的に求めた。

1. Introduction

The duality of the string theory, "the gauge/geometry correspondence", has been studied for a decade. It connects a gauge field theory and a geometry in the string theory. By using non-perturbative objects such as D-branes in the string theory it is possible to construct effective gauge theories living on them with various symmetries. Some of these gauge theories can be used as realistic models to explain accelerator experiments of particle physics or observations of the universe. On the other hand, geometries the non-perturbative objects produce around them could be related to known supergravities. These gauge theories and supergravities are expected to be related by a duality if the gauge theories have a large color symmetry and a large coupling. A large coupling constant is realized in the low energy limit in asymptotically free gauge theories such as QCD. The strong coupling regime of field theories is of course hard to analyze in general since the perturbative method, which is powerful in the weak coupling regime, is no longer valid. The gauge/geometry correspondence is conjectured to relate the strong coupling regime of field theories to the weak coupling theory of gravity. It provides a powerful tool to analyze non-perturbative properties of the strongly coupled field theories.

Many examples of the gauge/geometry correspondence are studied so far. Especially, the duality for gauge field theories with the conformal symmetry and the maximal supersymmetry is studied in detail and is called "the AdS/CFT correspondence" [1, 2, 3]. It relates conformal field theories (CFT) in four-dimensional spacetime to supergravity or the string theory in ten-dimensional spacetime containing the anti de-Sitter (AdS) spacetime. Although the direct proof of the AdS/CFT correspondence has not been given yet, there are many evidences supporting it.

A key to understand the duality is configurations of D-branes, which are nonperturbative objects in the string theory. D-branes are found at the ends of open strings and are surfaces which describe a whole trajectory of the string ends. Depending on their configurations in spacetime, D-branes can satisfy the BPS conditions and preserve a certain number of supersymmetries. D-branes can be

multiple, and their number N is related to the number of the color symmetry of the field theory living on the D-branes. If N is large enough, quantum effects of the dual string theory are small. Furthermore, if the coupling constant of the field theories is large enough, the dual string theory can be approximated by a supergravity. Therefore, a large N gauge theory with a large coupling constant can be described by a classical theory of supergravity.

The isometry of the AdS spacetime is interpreted as a conformal symmetry in the field theory side since they are described by the same group. The conformal symmetry, however, is not present in realistic field theories. Therefore, it is one of the tasks in applying the gauge/geometry correspondence to realistic models to generalize the AdS/CFT correspondence to the cases without the conformal symmetry. Despite this it is instructive to examine the AdS/CFT correspondence with the conformal symmetry in detail as a first step toward more realistic cases.

Certain combinations of operators in gauge theories called BMN operators were found to have a relation to the geometry called pp-wave spacetime, which is obtained by boosting the AdS spacetime at the light speed. The gauge/geometry correspondence for this geometry was studied by using the string theory itself [4, 5]. In the field theory side the spectrum of conformal dimensions of the BMN operators was obtained independently of the duality [6]. The BMN operators can be identified with spin chain models of the ferromagnet theory and were studied by using the Bethe ansatz method familiar in the condensed matter physics. To explain the results obtained in the field theory side in terms of the dual theory one needs the string theory itself instead of a supergravity approximation. So one needs to construct the superstring theory on the AdS background and study its properties in detail.

The construction of the string theory in the AdS spacetime has been a long wishing project since the original AdS/CFT correspondence was proposed. Metsaev and Tseytlin [7] constructed the Green-Schwarz type action of the type IIB superstring in $AdS_5 \times S^5$ as a sigma model with a coset target space $PSU(2, 2|4)/[SO(4,1) \times SO(5)]$. Then the light-cone gauge-fixings of the κ -symmetry and reparametrizations on the worldsheet were discussed in refs. [8, 9].

In this paper we discuss the global symmetry of the type IIB superstring in $\text{AdS}_5 \times S^5$ by using a group theoretical method. The symmetry is represented by the supergroup $\text{PSU}(2, 2|4)$. We use the worldsheet action of ref. [8] where the κ -symmetry is fixed by the light-cone gauge. We obtain explicit forms of the transformation laws for the symmetry $\text{PSU}(2, 2|4)$. The transformation laws we obtain will be useful in constructing the Noether charges for this symmetry [9]. They are also useful in finding consistent truncations of the theory, which are need in some investigations of the gauge/string correspondence [6, 10, 11].

2. IIB superstring in $\text{AdS}_5 \times S^5$

The type IIB superstring in $\text{AdS}_5 \times S^5$ can be described [7] as a sigma model with a target space $\text{PSU}(2, 2|4)/[\text{SO}(4,1) \times \text{SO}(5)]$. The supergroup $\text{PSU}(2, 2|4)$ contains a bosonic subgroup $\text{SO}(4,2) \times \text{SO}(6)$, which is the isometry of $\text{AdS}_5 \times S^5$. Its generators are

$$P^a, J^{ab}, D, K^a, J^I, Q^{\pm i}, S^{\pm i}, \quad (1)$$

where P^a, J^{ab}, D, K^a are $\text{SO}(4,2)$ generators, J^I are $\text{SU}(4) \sim \text{SO}(6)$ generators, and $Q^{\pm i}, S^{\pm i}$ are supercharges. Here, $a, b, \dots = 0, 1, 2, 3$ and $i, j, \dots = 1, 2, 3, 4$ denote $\text{SO}(3,1)$ and $\text{SU}(4)$ indices. The (anti-)commutation relations of these generators are given in ref. [8], whose conventions we use throughout this paper. The generators of the subalgebra $\text{SO}(4,1) \times \text{SO}(5)$ are

$$J^{ab}, \hat{J}^{4a} = K^a + \frac{1}{2}P^a, \quad J^{A'B'} = -\frac{1}{2}(\gamma^{A'B'})^j{}_i J^I_j, \quad (2)$$

where $A', B' = 1, 2, 3, 4, 5$ are $\text{SO}(5)$ indices and $\gamma^{A'}$ are $\text{SO}(5)$ gamma matrices. We use the light-cone coordinates $x^\pm = \frac{1}{\sqrt{2}}(x^3 \pm x^0)$, $x = \frac{1}{\sqrt{2}}(x^1 + ix^2)$, $\bar{x} = \frac{1}{\sqrt{2}}(x^1 - ix^2)$ and define $P = P^x$, $\bar{P} = P^{\bar{x}}$, $K = K^x$, $\bar{K} = K^{\bar{x}}$.

We choose a representative of the coset space $\text{PSU}(2, 2|4)/[\text{SO}(4,1) \times \text{SO}(5)]$ as

$$\begin{aligned}
G = & \exp(x^a P_a) \exp(\theta^{-i} Q_i^+ + \theta^{-i} Q_i^{+i} + \theta^{+i} Q_i^- + \theta^{+i} Q_i^{-i}) \\
& \times \exp(\eta^{-i} S^+ + i + \eta^{-i} S^+ + i + \eta^{+i} S^- + i + \eta^{+i} S^- + i) \exp(\phi D) \\
& \times \exp\left(\frac{1}{2} i y^{A'} (\gamma^{A'})^i{}_j J^j{}_i\right),
\end{aligned} \tag{3}$$

where $\theta_i^\pm = (\theta^{\pm i})^\dagger$, $Q_i^\pm = (Q^{\pm i})^\dagger$, etc. The variables $x^a, \phi, y^{A'}, \theta^{\pm i}, \eta^{\pm i}$ are coordinates of the coset space. We then fix the κ -symmetry by the light-cone gauge condition

$$\theta^{+i} = \eta^{+i} = 0 \tag{4}$$

and put $\theta^{-i} = \theta^i$, $\eta^{-i} = \eta^i$ for simplicity. The left-invariant Cartan 1-forms $\{L\}$ are defined by

$$\begin{aligned}
G^{-1} dG = & L_P^a P_a + \frac{1}{2} L^{ab} J^{ab} + L_D D + L_K^a K_a + L_J^i J_i + L_Q^i Q_i^+ + L_{\bar{Q}}^i Q_i^{+i} \\
& + L_Q^{+i} Q_i^- + L_{\bar{Q}}^{+i} Q_i^{-i} + L_S^i S_i^+ + L_{\bar{S}}^i S_i^{+i} + L_S^{+i} S_i^- + L_{\bar{S}}^{+i} S_i^{-i}
\end{aligned} \tag{5}$$

Using the explicit forms of the Cartan 1-forms the world-sheet action in the lightcone gauge was obtained in ref. [8].

3. PSU(2, 2|4) transformations

According to the general theory of the nonlinear realization [12, 13] the PSU(2, 2|4) transformation of the representative (3) is

$$G \rightarrow G' = g G h^{-1}(g), \tag{6}$$

where g is an arbitrary element of PSU(2, 2|4), and $h(g)$ is a compensating SO(4,1) \times SO(5) transformation which is chosen such that G' has a form in eq. (3). After the light-cone gauge fixing of the κ -symmetry (4) we also need a compensating κ -transformation. An infinitesimal PSU(2, 2|4) transformation is thus written as

$$G^{-1} \delta G = G^{-1} \epsilon G - \sigma(\epsilon) + G^{-1} \delta_\kappa G, \tag{7}$$

where ϵ is an arbitrary element of the PSU(2, 2|4) algebra

$$\begin{aligned} \epsilon = & \zeta^a P^a + \frac{1}{2} \tilde{\lambda}^{ab} J^{ab} + \Lambda D + \zeta^a K^a + \nu^j J_j + \epsilon^{-i} Q_i^+ + \epsilon_i^- Q^{+i} \\ & + \epsilon^{+i} Q_i^- + \epsilon_i^+ Q^{-i} + \beta^{-i} S_i^+ + \beta_i^- S^{+i} + \beta^{+i} S_i^- + \beta_i^+ S^{-i}, \end{aligned} \quad (8)$$

$\sigma(\epsilon)$ is a compensating $\text{SO}(4,1) \times \text{SO}(5)$ transformation

$$\sigma(\epsilon) = \frac{1}{2} \tilde{\lambda}^{ab} J^{ab} + \zeta^a \left(K^a + \frac{1}{2} P^a \right) + \frac{1}{2} \tilde{\nu}^{A'B'} J^{A'B'}, \quad (9)$$

and the last term is a compensating κ -transformation. The parameters ζ^a , $\tilde{\lambda}^{ab}$, $\tilde{\nu}^{A'B'}$ and those of the κ -transformation depend on ϵ . The κ -transformation has a form [7]

$$\begin{aligned} G^{-1} \delta_\kappa G = & \hat{\kappa}_{Q_i}^{-i} Q_i^+ + \hat{\kappa}_{Q_i}^+ Q^{-i} + \hat{\kappa}_{Q_i}^+ Q_i^- + \hat{\kappa}_{Q_i}^- Q^{-i} \\ & \hat{\kappa}_{S_i}^{-i} S_i^+ + \hat{\kappa}_{S_i}^+ S^{-i} + \hat{\kappa}_{S_i}^+ S_i^- + \hat{\kappa}_{S_i}^- S^{-i} + (J^{ab}, J^{A'B'} \text{ terms}). \end{aligned} \quad (10)$$

The coefficients in the present convention are given by

$$\begin{aligned} \hat{\kappa}_Q^{+i} = & -2 [\hat{L}_\mu^+ \kappa_S^{\mu 1i} + \hat{L}_\mu^x \kappa_S^{\mu 2i} - i \hat{L}_\mu^4 \kappa_{Q1}^{\mu i} + L_\mu^{A'} (\gamma^{A'})^i_j \kappa_{Q1}^{\mu j}], \\ \hat{\kappa}_Q^{-i} = & 2 [-\hat{L}_\mu^- \kappa_S^{\mu 2i} + \hat{L}_\mu^x \kappa_S^{\mu 1i} - i \hat{L}_\mu^4 \kappa_{Q2}^{\mu i} + L_\mu^{A'} (\gamma^{A'})^i_j \kappa_{Q2}^{\mu j}], \\ \hat{\kappa}_S^{+i} = & 2 [-2i \hat{L}_\mu^+ \kappa_{Q2}^{\mu i} + 2i \hat{L}_\mu^x \kappa_{Q1}^{\mu i} + \hat{L}_\mu^4 \kappa_S^{\mu 2i} - i L_\mu^{A'} (\gamma^{A'})^i_j \kappa_S^{\mu 2j}], \\ \hat{\kappa}_S^{-i} = & 2 [2i \hat{L}_\mu^- \kappa_{Q1}^{\mu i} + 2i \hat{L}_\mu^x \kappa_{Q2}^{\mu i} + \hat{L}_\mu^4 \kappa_S^{\mu 1i} - i L_\mu^{A'} (\gamma^{A'})^i_j \kappa_S^{\mu 1j}], \end{aligned} \quad (11)$$

where $\mu = 0, 1$ is a world index on the worldsheet and κ 's on the right-hand sides are independent transformation parameters.

For general variations of the variables $(x^a, \phi, \theta^i, \eta^i)$ the variation of G in eq. (3) is given by

$$\begin{aligned} G^{-1} \delta G = & e^\phi \delta x^+ P^- + e^{+\phi} \left[\delta x^- - \frac{1}{2} i (\theta^i \delta \theta_i + \theta_i \delta \theta^i) \right] P^+ + e^\phi \delta x \tilde{P} + e^\phi \delta \bar{x} P \\ & + e^{-\phi} \left[\frac{1}{4} (\eta^2)^2 \delta x^+ + \frac{1}{2} i (\eta^i \delta \eta_i + \eta_i \delta \eta^i) \right] K^+ + \delta \phi D \\ & + \left[(\delta U U^{-1})^i_j + i \left(\tilde{\eta}^i \tilde{\eta}_j - \frac{1}{4} \eta^2 \delta^i_j \right) \delta x^+ \right] J_j^i + e^{\frac{1}{2}\phi} (\tilde{\delta} \theta^i + i \tilde{\eta}^i \delta x) Q_i^+ \\ & + e^{\frac{1}{2}\phi} (\tilde{\delta} \theta_i - i \tilde{\eta}_i \delta \bar{x}) Q^{+i} - i e^{\frac{1}{2}\phi} \tilde{\eta}^i \delta x^+ Q_i^- + i e^{\frac{1}{2}\phi} \tilde{\eta}_i \delta x^+ Q^{-i} \\ & + e^{-\frac{1}{2}\phi} (\tilde{\delta} \eta^i + \frac{1}{2} i \eta^2 \tilde{\eta}^i \delta x^+) S_i^+ + e^{-\frac{1}{2}\phi} (\tilde{\delta} \eta_i - \frac{1}{2} i \eta^2 \tilde{\eta}^i \delta x^+) S^{+i}, \end{aligned} \quad (12)$$

where we have used the explicit forms of the Cartan 1-form in the light-cone gauge given in ref. [8]. U_j^i is the $\text{SU}(4)$ matrix determined by the coordinates $y^{A'}$ and $\tilde{\theta}^i =$

U^i, θ^i , etc. The compensating transformations in eq. (7) are chosen such that the total transformation has this form.

We are now ready to obtain explicit forms of the PSU(2, 2|4) transformations. The transformations for P^a , D , J^{+-} , J^{+x} , $J^{x\bar{x}}$, $J^{A'B'}$ and Q^+ do not need compensating κ -transformations and are easy to obtain. They were already given in ref. [9]. For instance, the transformations for P^a and Q^+ are

• P^a transformations:

$$\delta x^a = \zeta^a, \quad \delta(\text{others}) = 0. \quad (13)$$

• Q^{+i} transformations:

$$\delta x^- = \frac{1}{2} i \epsilon^-_i \theta^i + \frac{1}{2} i \epsilon^{-i} \theta_i, \quad \delta \theta^i = \epsilon^{-i}, \quad \delta(\text{others}) = 0. \quad (14)$$

The transformations for K^+ do not need a compensating κ -transformation either. We obtain

• K^+ transformations:

$$\begin{aligned} \delta x^a &= \zeta^-(x^+ x^a - \frac{1}{2} x \cdot x \eta^{a+} - \frac{1}{2} e^{-2\phi} \eta^{a+}), \quad \delta \phi = -\zeta^- x^+, \\ \delta \eta^i &= -\zeta^- x^+ \eta^i, \quad \delta(\text{others}) = 0. \end{aligned} \quad (15)$$

Other transformations need compensating κ -transformations and are more involved. We have obtained all of these transformations. Here we give only the transformation for Q^- . The remaining transformations will be given in ref. [14].

• Q^{-i} transformations:

$$\begin{aligned} \delta x^+ &= 0, \quad \delta x = i \epsilon^+_i \theta^i, \quad \delta \phi = -\frac{1}{2} (\epsilon^+_i \eta^i - \epsilon^{+i} \eta_i), \\ \delta x^- &= \frac{1}{2} i e^{-\frac{1}{2}\phi} (\tilde{\theta}^i \hat{\kappa}_{\tilde{Q}^i} + \tilde{\theta}^i \hat{\kappa}_{\tilde{Q}^{-i}}) + \frac{1}{4} i e^{-\frac{1}{2}\phi} (\tilde{\eta}^i \hat{\kappa}_{S^i} + \tilde{\eta}_i \hat{\kappa}_{S^{-i}}) \\ &\quad + \frac{1}{8} i e^{-2\phi} \eta^2 (\epsilon^+_i \eta^i + \epsilon^{+i} \eta_i), \\ (\delta U U^{-1})^i_j &= -(\tilde{\epsilon}^+_j \tilde{\eta}^i + \tilde{\epsilon}^{+i} \tilde{\eta}_j) - (\text{trace part}), \\ \tilde{\delta} \theta^i &= e^{-\frac{1}{2}\phi} \hat{\kappa}_{\tilde{Q}^{-i}}, \quad \tilde{\delta} \eta^i = e^{-\frac{1}{2}\phi} \hat{\kappa}_{S^{-i}} - \epsilon^+_j \eta^j \tilde{\eta}^i - \frac{1}{2} \eta^2 \tilde{\epsilon}^{+i} \end{aligned} \quad (16)$$

To obtain the form (12) we need to choose the parameters of the κ -transformation as

$$\hat{\kappa}_Q^{+i} = -e^{+i\phi} \tilde{\epsilon}^{+i}, \quad \hat{\kappa}_S^{+i} = 0. \quad (17)$$

From these conditions and eq. (11) the parameters $\hat{\kappa}_Q^{-i}$, Q , $\hat{\kappa}_S^{-i}$ in the transformation (16) are determined as

$$\begin{aligned} \hat{\kappa}_Q^{-i} &= \frac{1}{2} e^{+i\phi} \left(\frac{\partial_- x}{\partial_- x^+} + \frac{\partial_+ x}{\partial_+ x^+} \right) \tilde{\epsilon}^{+i}, \\ \hat{\kappa}_S^{-i} &= \frac{1}{2} i e^{-i\phi} \left(\frac{\partial_- \phi}{\partial_- x^+} + \frac{\partial_+ \phi}{\partial_+ x^+} \right) \tilde{\epsilon}^{+i} + \frac{1}{2} e^{-i\phi} (\gamma^{A'})^i_j \left(\frac{L_-^{A'}}{\partial_- x^+} + \frac{L_+^{A'}}{\partial_+ x^+} \right) \tilde{\epsilon}^{+i}, \end{aligned} \quad (18)$$

where

$$L_{\pm}^{A'} = \frac{1}{2i} (\gamma^{A'})^i_j \left[(\partial_{\pm} U U^{-1})^i_j + i \left(\tilde{\eta}^i \tilde{\eta}_j - \frac{1}{4} \eta^2 \delta_j^i \right) \partial_{\pm} x^+ \right]. \quad (19)$$

From eq. (16) we see that the Q^- transformation of x^+ vanishes. This means in particular that the commutator of two Q^- transformations is zero on x^+ , which at first sight looks inconsistent with the PSU(2, 2|4) algebra

$$\{Q^{-i}, Q_j^-\} = iP \delta_j^i. \quad (20)$$

This apparent inconsistency can be resolved as follows. Since we have not fixed a gauge for reparametrizations on the worldsheet, the commutator algebra closes up to reparametrizations. The commutator of two Q^- transformations on x is

$$[\delta_{Q^-}(\epsilon_1^+), \delta_{Q^-}(\epsilon_2^+)]x = (\zeta^- \partial_- + \zeta^+ \partial_+)x, \quad (21)$$

which is a reparametrization with the parameters

$$\zeta_{\pm} = \frac{1}{2\partial_{\pm} x^+} i(\epsilon_{2i}^+ \epsilon_1^{+i} - \epsilon_{1i}^+ \epsilon_2^{+i}). \quad (22)$$

As the reparametrization of x^+ is

$$(\zeta^- \partial_- + \zeta^+ \partial_+)x^+ = i(\epsilon_{2i}^+ \epsilon_1^{+i} - \epsilon_{1i}^+ \epsilon_2^{+i}), \quad (23)$$

the commutator can be written as

$$[\delta Q_-(\epsilon_1^+), \delta Q_-(\epsilon_2^+)]x^+ = -i(\epsilon_{2i}^+ \epsilon_1^{+i} - \epsilon_{1i}^+ \epsilon_2^{+i}) + (\zeta^- \partial_- + \zeta^+ \partial_+)x^+. \quad (24)$$

The first term on the right-hand side is a P^- transformation of x^+ expected from the $PSU(2, 2|4)$ algebra.

References

- [1] J. Maldacena, The large N limit of superconformal field theories and supergravity, *Adv. Theor. Math. Phys.* **2** (1998) 231 [arXiv:hep-th/9711200].
- [2] S.S. Gubser, I.R. Klebanov and A.M. Polyakov, Gauge theory correlators from non-critical string theory, *Phys. Lett.* **B428** (1998) 105 [arXiv:hep-th/9802109].
- [3] E. Witten, Anti de Sitter space and holography, *Adv. Theor. Math. Phys.* **2** (1998) 253 [arXiv:hep-th/9802150].
- [4] D. Berenstein, J. Maldacena and H. Nastase, Strings in flat space and pp waves from $N = 4$ super Yang Mills, *JHEP* **0204** (2002) 013 [arXiv:hep-th/0202021].
- [5] S.S. Gubser, I.R. Klebanov and A.M. Polyakov, A semi-classical limit of the gauge/string correspondence, *Nucl. Phys.* **B636** (2002) 99 [arXiv:hep-th/0204051].
- [6] N. Beisert, The dilatation operator of $N = 4$ super Yang-Mills theory and integrability, *Phys. Rept.* **405** (2005) 1 [arXiv:hep-th/0407277].
- [7] R.R. Metsaev and A.A. Tseytlin, Type IIB superstring action in $AdS_5 \times S^5$ background, *Nucl. Phys.* **B533** (1998) 109 [arXiv:hep-th/9805028].
- [8] R.R. Metsaev and A.A. Tseytlin, Superstring action in $AdS_5 \times S^5$: κ - symmetry light cone gauge, *Phys. Rev.* **D63** (2001) 046002 [arXiv:hep-th/0007036].
- [9] R.R. Metsaev, C.B. Thorn and A.A. Tseytlin, Light-cone superstring in AdS space-time, *Nucl. Phys.* **B596** (2001) 151 [arXiv:hep-th/0009171].
- [10] A.A. Tseytlin, Semiclassical strings and AdS/CFT, arXiv:hep-th/0409296.
- [11] L.F. Alday, G. Arutyunov and S. Frolov, New integrable system of 2dim fermions from strings on $AdS_5 \times S^5$, *JHEP* **0601** (2006) 078 [arXiv:hep-th/0508140].
- [12] S. Coleman, J. Wess and B. Zumino, Structure of phenomenological Lagrangians. 1, *Phys. Rev.* **177** (1969) 2239.
- [13] C.G. Callan, S. Coleman, J. Wess and B. Zumino, Structure of phenomenological Lagrangians. 2, *Phys. Rev.* **177** (1969) 2247.
- [14] M. Nishimura and Y. Tanii, to appear.